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## An Efficient Method for Road Tracking from Satellite Images Using Hybrid Multi-Kernel Partial Least Square Analysis and Particle Filter\*

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The Road extraction from the remotely sensed imagery is highly realistic for the quick road updating in the Geographic Information System (GIS) data collection. The particle filter (PF) was earlier employed to track the road maps in satellite images. In our previous work, we have introduced an efficient Gauss–Hermite Kalman Filter with Locally Excitatory Globally Inhibitory Oscillator Networks (GHKF–LEGION)-based road extraction, even though it does not properly extract the road from the complex region. In order to recover the track of the road beyond obstacles, in this work, we proposed a novel hybrid multi-kernel partial least squares (PLS) with PF approach. Here, at first, we estimate the initial leader point of the road employing the K-means clustering technique. Subsequently, the PF traces a road till a stopping benchmark is satisfied. Thereafter, without finishing the process, the outcomes are furnished to the hybrid kernel PLS technique which attempts to locate the continuance of the road after several potential road blocks or to locate the entire feasible road branches which are on the other side of the road junction. The outcomes are offered for five satellite images. The experimental results show our proposed road tracking method is better compared to other existing works.

**Keywords:**

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## 1 1. Introduction

3 There is no second opinion on the fact that, nowadays, a network of roads has  
5 emerged as an indispensable medium of transport and it constitutes one of the four  
7 pillars of human civilization. With the result, it has become highly essential to  
9 preserve and restore roads to maintain the transport network duly linked. The roads  
11 habitually take the shape of dark lines when observed from the satellite images which  
13 are by and largely accurate in the rural and suburban scenarios.<sup>1</sup> Of late, the road  
15 extraction from the satellite imagery has become the cynosure of attention and  
17 attraction among the investigating community. It is especially deployed in the city  
19 planning, cartography and to renovate the earlier identified roads in the Geographic  
21 Information Systems (GIS) settings.<sup>2</sup> The urban road mapping from the high spatial  
23 resolution images constitutes an invaluable as they facilitate the distinction of urban  
characteristics, though they bring in their train a host of novel issues as a number of  
the urban characteristics may be deemed as part and parcel of noise.<sup>3</sup> Habitually, the  
semiautomatic techniques function either as road followers identical to the techni-  
ques proposed in Refs. 5 and 6, or as the concurrent curve-fitting trackers such as the  
techniques based on active contour models,<sup>4</sup> piecewise parabola fitting,<sup>7</sup> and dy-  
namic programming (DP) optimization.<sup>8</sup> Even then, the automated methods gen-  
erally need the skilled integration of the contextual data and *a priori* knowledge in  
the road extraction process.<sup>3,9</sup> Several novel techniques were brought to spotlight  
intended for the assessment of the tracking of the road during the course of the last  
decade.<sup>10,11</sup> It is very essential for several applications to update and revise the road  
network data.

25 A homogeneity characteristic of the pixel was employed to extort the road feature  
27 from the satellite images.<sup>12</sup> The gradient operation-based<sup>13</sup> road skeletal formation  
29 was appropriate for the rural roads. The road extraction by level segmentation and  
31 morphological function<sup>14</sup> were performed on high-resolution satellite images. Nev-  
33 ertheless, the perfect automation of the road extraction procedures continues to be a  
35 hard nut to crack and is evading solutions with a logical degree of success (accuracy)  
37 over a titanic set of images of diverse types of urban and suburban scenarios. In this  
39 regard, one of the significant classes of road-tracking (RT) techniques is dependent  
41 on the probabilistic modeling of related data and Bayesian evaluation method, where  
statistical models are employed to represent the distinctiveness of the road features.  
As a rule, the captioned methods encompass two phases such as the prediction phase  
and update phase. The technique dependent on the extended Kalman filter (EKF)  
represents one of the vital techniques in this class, which was kickstarted for the road  
map extraction in Ref. 15 and thereafter was again renovated in Refs. 3 and 6. The  
particle filters (PFs) are usually employed for the nonlinear filtering. The techniques  
based on the PF were employed in Refs. 16 and 17 to trace a single road path  
initiated by a specified seed at the commencement of the road. One of the glaring  
defects in the prior works linked with the above-cited class of road extraction

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1 techniques<sup>3,6,15-17</sup> lies on the restricted processing area on the image. The corre-  
 3 sponding techniques utilize either EKF or PF, begin tracing a road from a specified  
 seed point on the road, and generally stop when they arrive at a stern occlusion, an  
 intersection, or even remarkable change in the road direction.

5 In the past few years, a feast of novel techniques has been given the green signal to  
 7 successfully address the recognition of roads from the satellite images. Standing out  
 amongst them are the knowledge-based techniques, mathematical morphology,<sup>18-20</sup>  
 9 snakes,<sup>3,21</sup> classification,<sup>22</sup> differential geometry,<sup>23</sup> region competition,<sup>24</sup> active  
 testing,<sup>25</sup> perceptual grouping<sup>26</sup> and the DP.<sup>27</sup> Further, the representative work  
 11 under the Bayesian structure may be broadly categorized into two types: (a) the  
 state evaluation for the linear and Gaussian model employing the Kalman filter and  
 13 its variants like the fragrance-free Kalman filter and comprehensive Kalman filter,  
 and (b) the state evaluation for the nonlinear and non-Gaussian challenge by  
 15 deploying the sequential Monte Carlo approaches<sup>28</sup> otherwise termed as the con-  
 densation filter,<sup>29</sup> bootstrap filter<sup>30</sup> and the PF.<sup>31,32</sup> The sterling merits of the se-  
 17 quential Monte Carlo approaches PF involve the scaling down of the sampling  
 patches in the course of the tracking and its incredible skills of effectively addressing  
 19 multi-modal distribution created by cluttered scenario. The advancement or aug-  
 mentation of the semiautomatic methods is highly essential to facilitate the quick,  
 21 reliable and accurate furnishing of the data for the GIS techniques like the complete,  
 or just approximately complete, mechanized procedures which have not failed to  
 23 turn the corner and become sufficiently mature.<sup>33</sup>

## 25 2. Related Works

27 It is worth mentioning that a feast of relevant investigations have been carried out by  
 the disinterested investigators with the intention of the extraction of satellite images.  
 Table 1 illustrates the evaluation of a few modern associated works regarding the  
 29 extortion of the satellite images. A road tracker, based on angular texture signature,  
 was kickstarted by Shen *et al.*<sup>34</sup> in accordance with skills acquired regarding the  
 31 roads on high-resolution imagery. The existing stipulations implied that the tech-  
 nique would meet with failure on a road cast by incredibly shadow and occlusion in  
 33 complicated scenarios. It was only capable of tracking the long ribbon roads on  
 grayscale imagery, requiring excessive evaluation time. The outcomes were exhibited  
 35 by means of a single high-resolution satellite image sample. The mean-shift clustering  
 technique was effectively employed within the hue-saturation-intensity space. The  
 37 conditional morphological approaches were utilized to considerably perk up the  
 segmentation outcomes in Ref. 35. A model and a strategy dependent on the multi-  
 39 scale recognition of the roads in juxtaposition with the geometry-constrained edge  
 extraction making use of the snakes were offered in Ref. 36. Outcomes were exhibited  
 41 for three sample images, and the related technique was invariably meant for the rural  
 areas. A host of coordinating snakes,<sup>37</sup> which were competent to split, merge and

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 $W_k^i$ ,  $W_k^i$  to  $W_k^i$ ,  
 $W_k^i$

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Table 1. Summary of related methods in road extraction.

Methods	Feature	Number of samples used as test case
Road tracker, angular texture signature <sup>34</sup>	Intensity and edge detection	2–4
Mean shift clustering <sup>35</sup>	Histogram of HSI image	1–8
Snakes <sup>36</sup>	Intensity gradient	3
SVM <sup>38</sup>	Intensity, edge gradient, edge length, width	3–6
Region competition <sup>28</sup>	Intensity	4
Binarization, optimization using Markov random field <sup>39</sup>	Mean radiance value	5
Perceptual grouping algorithm <sup>41</sup>	Intensity, edge	2–3
Toe finding algorithm <sup>42</sup>	Intensity, shape	3–4
Fast linear feature detector algorithm <sup>11</sup>	Intensity, linear features	2
Multi-scale geometric analysis of detector responses <sup>12</sup>	Shape, road point	1
DP algorithm <sup>43</sup>	Direction, radiometric information	2
Unscented kalman filter (UKF) and gauss–hermite kalman filter (GHKF) (previous work) <sup>45</sup>	Shapes, color, intensity	3
Locally excitatory globally inhibitory oscillator networks (LEGION) and GHKF (previous work) <sup>46</sup>	Shapes, color, intensity	3
Ours proposed work	Shapes, color, intensity	5

disappear as and when needed were employed to extort the detached road networks and the enclosed areas. The energy functional consisted of the gradient vector flow evaluated as a diffusion of the gradient vectors of a gray level or binary edge map attained from the image.

A Lion’s share of the modern road extraction approaches for multi-spectral imagery invariably depends on a mechanized and consistent classification of road surfaces. However, it is unfortunate that the classification precision of roads fares poorly irrespective of whether a supervised or unsupervised classification technique is used. The cardinal roadblock is related to the excessive misclassification between the roads and the spectrally analogous objects including the parking lots, buildings, crop fields, to name a few. Song and Civco<sup>38</sup> effectively employed two shape measures such as the smoothness and compactness to considerably decrease the misclassification between roads and other spectrally identical objects in a support vector machine (SVM) classifier. Further, Amo *et al.*<sup>28</sup> were instrumental in launching the road extraction employing the region competition technique. An initial simple model was distorted by means of the region growing algorithms to achieve a coarse road approximation. This model was improved by regional competition. In Ref. 39, Negri *et al.* convincingly discussed explained the junction-aware extraction and regularization of the urban road networks in high-resolution synthetic aperture radar (SAR) images, although the technique met with a waterloo in its role as the road detector.

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1 Sahar and Alireza<sup>40</sup> amazingly launched a significant road tracing technique making  
3 use of the comprehensive Kalman filter and a special PF module. These modules,  
5 employing the clustering techniques, were capable of overcoming all the hindrances  
7 on the road and track all the road branches at a junction. In fact, all road segments in  
9 a linked road network were tracked by means of a single seed point. Nevertheless, the  
11 efficiency of the technique solely depended on the parameters of the module. A novel  
13 technique was green-signaled and implemented by Paolo Gamba *et al.*<sup>41</sup> for detecting  
15 the urban road networks from the high-resolution optical/SAR images. The per-  
17 ceptual grouping technique was employed to recoup the local flaws and also to  
19 rebuild the normal roads in the images. The vital constraint of the innovative  
21 technique was the substandard precision as the overall precision range was a mere  
23 45.48%.

25 An automatic technique for extorting road from the aerial imagery was brought to  
27 the spotlight by Hu *et al.*<sup>42</sup> In view of the excessive extortion, the tracking of road  
29 footprints was adversely affected. With an eye on finding a solution to this hassle, an  
31 innovative method was envisaged by Shao *et al.*<sup>11</sup> for designing a quick and efficient  
33 technique for identifying the ridge- or ribbon-like linear features from the remote  
35 sensing imagery. The aerial images were deployed to verify the efficiency of the  
37 technique in the extortion of the roads. An innovative road network grouping  
39 technique was coined by He *et al.*<sup>12</sup> for the SAR images by employing the multi-scale  
41 geometric assessment of the detector feedbacks. The roadmap of the algorithm  
consisted of three stages. (1) the extraction of guidance segments, (2) segment la-  
beling and (3) the grouping of the road guidance segments. Further, a well-orches-  
trated semiautomatic technique for the 3D road extraction in rural areas employing  
the stereoscopic aerial images was envisaged by Dal Poz *et al.*<sup>43</sup> The appealing test  
outcomes illustrated without an iota of doubt that the innovative approach was  
skilled enough to usher in amazingly accurate road centerlines. A novel technique  
was flagged off by Miao *et al.*<sup>44</sup> to extort the road centerline from the high-resolution  
imagery depending on the shape features and the multi-variate adaptive regression  
splines (MARS). The cardinal constraint of captivating technique was that the  
thresholds in the technique had to be manually evaluated and that it was not the  
appropriate candidate for the low-resolution images.

33 **Considering the above challenges, an efficient approach is urgently needed to**  
35 **improve the road extraction limitations.** In this paper, we have proposed a road  
37 extraction approach to extract road region from the satellite images. Then, the  
39 performance of the procedure is tested on five different satellite images. The rest of  
41 the paper is organized as follows. Introduction is explained in Secs. 1 and 2  
explains the related works. The design strategy of proposed method is explained in  
Sec. 3 and justification of the different stages for RT process is explained in Sec. 4.  
Result and discussion are provided in Sec. 5, finally, the conclusion is summed up  
in Sec. 6.

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### 1 **3. Design Strategy and Proposed Methodology for RT**

#### 3 **3.1. Road design**

5 The grave challenges in the design of an automated road network extraction  
 7 mechanism employing the remotely sensed imagery lie in the fact that the image  
 9 traits of road feature change depending on the sensor type, spectral and spatial  
 11 resolution, ground traits and so on. Even with respect to an image obtained over a  
 specific urban region, diverse segments of the road network expose diverse features.  
 In the actual world, a road network is so complicated that it is very difficult to model  
 by means of a mathematical formulation or a theoretical structural model. The  
 existence of other objects such as the buildings and trees emits shadows to occlude  
 road features, thereby making the extraction procedure further complex.

13 The human perceptual methods of identifying a road include<sup>48</sup> the extraction of  
 the geometric, radiometric and topological features of an image. The human beings  
 15 habitually identify a road deploying initially its geometric features, creating a road to  
 be an extensive and stretched out feature with identical width and analog radio-  
 17 metric variation all through its path. Though the spectral features of a road fluctuate  
 within an image, its physical appearance tends to exist with the elongated and  
 19 incessant traits. The human beings blend these critical clues to locate a foreground  
 road object from the background layer. This phenomenon has motivated us to design  
 21 a generic structure which integrates the appropriate processing modules essential for  
 the extortion of various categories of features available in the road objects from  
 23 satellite scenes. In the configuration of the RT issue, as in Ref. 2, we employ a 4D  
 state vector as follows:

$$25 \quad U_K = [R_k \ C_k \ \Phi_k \ \overline{\Phi}_k],$$

27 where  $R_k$  is row of the center of the road,  $C_k$  is column of the center of the road,  $\Phi_k$  is  
 road direction and  $\overline{\Phi}_k$  is change in road direction.

29 These roads are endowed with a characteristically distinct spectral signature  
 locally and universally in relation to the background layer such as the vegetation,  
 31 soil, waterways and the synthetic structures, to name a few. The corresponding road  
 framework is fruitfully employed in our technique.

#### 33 **3.2. Design of PF**

35 The PF was kickstarted in 1993 by Gordon as the bootstrap filter for evaluation of  
 the nonlinear and non-Gaussian states.<sup>47</sup> In the PF, the state at each time instant  
 37 is characterized by sample-based probability density function (PDF). The se-  
 quential Monte Carlo technique with significant sampling is elegantly employed for  
 39 the evaluation of the nonlinear and non-Gaussian state. The underlying motive of  
 the PF is to evaluate the state of the system by means of the weighted mean of  
 41 particles available in the vicinity of state space. It represents a recursive procedure

1 where the prior state is revised by means of the online measurements (weights) to  
 2 ascertain the subsequent state evaluation. When the evaluation of a subsequent  
 3 state is finished, it functions as prior for the succeeding state evaluation. The  
 4 weights in the PF represent probability measure between the posterior probability  
 5 density and reference prior probability density. Even though the PF concept is  
 6 voluminously discussed in the literature, we have given an introduction of the PF  
 7 concept with a concise description solely for the purpose of the conclusion of the  
 8 research document.

9 For the evaluation of the subsequent state of the mechanism, the target model is  
 10 shortlisted which demarcate various features such as the motion, scaling, rotation  
 11 factor for the target. In accordance with Eq. (1), the target model is configured.

$$12 \quad U_K = H_{K-1}(U_{K-1}, M_{K-1}). \quad (1)$$

13 Here,  $H_{K-1} : R^m \times R^n \rightarrow R^m$  is the nonlinear function of target state with a  
 14 dimension of  $m$ ;  $M_{k-1} \in R^n$  is white noise sequence of dimension  $n$  with zero mean  
 15 (known PDF) represents the uncertainty in state prediction. Also, online discrete  
 16 measurement  $V_K \in R^v$ ,  $K \geq 1$  up to current time  $K$  are made according to mea-  
 17 surement Eq. (2)

$$18 \quad V_K = G_K(U_K, Z_K), \quad (2)$$

19 where  $G_K : R^k \times R^q \rightarrow R^v$  is a nonlinear function,  $Z_K$  is zero mean, white noise  
 20 sequence (PDF known) representing an error in measurements. Recursive process of  
 21 PF consists of two steps as (i) prediction, (ii) updating from the given online mea-  
 22 surement sequences  $V_K = \{V_i : i = 1, 2, \dots, K\}$ . In prediction step, prior PDF at  
 23 time instant  $K$  is determined as

$$24 \quad P(U_K|V_{K-1}) = \int P(U_K|U_{K-1})P(U_{K-1}|V_{K-1})dU_{K-1}, \quad (3)$$

25 where in Eq. (3) prior PDF is obtained using system model Eq. (1) and initial PDF at  
 26 time  $K - 1$ , i.e.,  $P(U_{K-1}|V_{K-1})$ . In update step, the problem is to estimate the  
 27 posterior density  $P(U_{0:K}|V_{1:K})$  using the Bayes rules as defined in Eq. (4) at every  
 28 time-step is given in the prior PDF  $P(U_0|V_1) \equiv P(U_1)$  functional form of state ( $H$ )  
 29 and measurement ( $G$ ) up to that time instant. The same can be expressed as

$$30 \quad P(U_K|V_K) = \frac{P(V_K|V_{0:K})P(V_K|V_{K-1})}{P(V_K|V_{K-1})}. \quad (4)$$

31 **In PF, Eqs. (3) and (4) form the recursive process for state estimation.** Consid-  
 32 ering the tracking problem  $N$  random samples  $[U_1^{(i)}]_{i=1,2,\dots,N}$  are taken from initial  
 33 given PDF  $P(U_1)$ . These samples are passed through system state model equation (1)  
 34 in order to obtain predicted  $N$  particles. The predicted particles are assigned nor-  
 35 malized weights using Eq. (5).  
 36

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$$W_j = \frac{P(V_K|U_K(j))}{\sum_{j=1}^N P(V_K|U_K(j))}, \quad \text{where } j = 1, 2, \dots, N. \quad (5)$$

Because the target dynamics are assumed to be Markov chain, posterior can be represented as

$$P(U_K|V_{1:K}) \approx \sum_{j=1}^N W_K^j \delta(U_K - U_K^j), \quad (6)$$

where  $\delta(\bullet)$  represents the Dirac delta function on account of the deterministic nature of Eq. (1) for the specified value of  $U_{K-1}$  and  $W_{K-1}$ . At last, the revised particles function as the prior for the succeeding state prior particles and this recursive procedure goes on until the last state forecast and revision. If the dimension of the particle is enhanced, the precision of the tracking gets perked up, though it entails additional processing power. In actual practice, only a restricted number of particles are used for the tracking application. Further, after little state evaluation, the number of particles with negligible weights goes up and the upkeep of these tiny particles whose contribution to evaluation is trivial need added computational power. Hence, the resampling is initiated on revised particles so as to ignore the particles having insignificant weights.<sup>8</sup> In the resampling process, new samples  $[*U_K^i]_{i=1,2,\dots,N}$  are created by resampling  $N$  times from the evaluated PDF  $P(U_K|V_{1:K})$  in order that for any  $j$   $\Pr[*U_K^i = U_K^j]_{i=1,2,\dots,N} = W_K^j$ . The pseudo-code of the PF is furnished in Table 2.

Table 2. Pseudo-code for PF.

---

29	Input:
	Satellite image
	Parameters of PFs
31	1. For $j = 1 : N$
	2. At time $K = 1$
33	3. Randomly sample PDF $P(U_{K-1} V_{1:K-1})$ for selecting $N$ Samples $[U_{K-1}^{(i)}]_{i=1,2,\dots,N}$
	4. Assign weight to particle as per Eq. (5)
35	5. Calculate the sum of weight $W_{\text{sum}} = \sum_{i=1}^N W_i$
	6. Normalize the weight for particles.
37	7. Resample: generate new samples $[U_K^{(i)}, W_K^{(i)}]_{i=1,2,\dots,N}$ based upon $W_K^i$ after resampling of $N$ updated particles so that $\Pr[*U_K^{(i)} = U_K^j]_{i=1,2,\dots,N} = W_K^j$
39	8. Estimate the state by $U_K = \frac{1}{N} \sum_{i=1}^N X_k^i$
	9. $k + 1 \leftarrow k, j + 1 \leftarrow j$
	10. Go to Step 3
41	Output:
	Tracked road

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### 1 3.3. Design of partial least squares analysis

3 Partial least squares (PLS) analysis<sup>49</sup> represents a statistical technique for designing  
 5 the relations between sets of variables through certain latent quantities. In the PLS  
 7 evaluation, the observed data is deemed to be created by a procedure motivated by  
 9 an insignificant number of latent variables. Let  $U \in R^m$  represent an  $m$ -dimensional  
 11 space of variable and  $V \in R^n$  symbolize an  $n$ -dimensional space of other variables.  
 With  $N$  observed samples from each space  $u \in U$  and  $v \in V$  from the two block of  
 variables,  $U \in R^{N \times m}$  and  $V \in R^{N \times n}$ , PLS techniques locate new spaces where large  
 deviations of the observed samples can be maintained, and the skilled latent vari-  
 ables from the two blocks are highly associated vis-à-vis those in the original spaces,

$$13 \quad \begin{aligned} U &= XM^T + I, \\ V &= YN^T + J, \end{aligned} \quad (7)$$

15 where

17  $X \in R^{N \times p}, Y \in R^{N \times P} \rightarrow$  factor (score component) matrices,  
 19  $M \in R^{m \times p}, N \in R^{n \times p} \rightarrow$  loading matrices,  
 21  $I \in R^{N \times m}, J \in R^{N \times n} \rightarrow$  error terms,

To decompose  $U$  and  $V$  by Eq. (1), PLS algorithms first compute the weight  
 vectors  $a_1$  and  $b_1$  such that most variations in  $U$  and  $V$  can be retained by  $x_1 = Ua_1$   
 and  $y_1 = Vb_1$ .

$$23 \quad \begin{aligned} &\max_{a_1} |\text{Var}(x_1)|, \\ &\max_{b_1} \text{Var}(y_1), \end{aligned} \quad (8)$$

25 where

27  $x_1$  and  $y_1$  are first columns of  $X$  and  $Y$ ,  $\text{Var}(\bullet)$  is Variance.  
 Meanwhile, PLS analysis also requires  $x_1$  besting explaining  $y_1$

$$29 \quad \max_{a_1, b_1} \text{Var}(x_1, y_1), \quad (9)$$

31 where  $\rho(x_1, y_1) = \text{Cov}(x_1, y_1) / \sqrt{\text{Var}(x_1)\text{Var}(y_1)}$  defines the correlation coefficient  
 33 between  $x_1$  and  $y_1$  and  $\text{Cov}(x_1, y_1) = x_1 y_1 / N$  denotes the sample covariance between  
 35  $x_1$  and  $y_1$ . Combining Eqs. (2) and (3), PLS analysis maximizes the covariance  
 between  $x_1$  and  $y_1$  in the first step

$$37 \quad \max_{a_1, b_1} \text{Cov}(x_1, y_1) = \max_{a_1, b_1} \sqrt{\text{Var}(x_1)\text{Var}(y_1)} \rho(x_1, y_1). \quad (10)$$

39 Therefore,  $a_1$  and  $b_1$  can be computed by solving the following optimization problem:

$$41 \quad \begin{aligned} &\max \langle Ua_1, Vb_1 \rangle, \\ &st \ a_1^T a_1 = 1, \quad b_1^T b_1 = 1, \end{aligned} \quad (11)$$

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1 where  $\langle Ua_1, Vb_1 \rangle$  denotes the inter-product of  $Ua_1$  and  $Vb_1$ . The optimal weight  
 3 vector  $a_1$  for above optimization problem is the first eigenvector of the following  
 eigenvector problem<sup>19</sup>:

$$5 \quad U^T V V^T U a_1 = \lambda a_1. \quad (12)$$

7 Similarly,  $b_1$  can be obtained by solving another eigenvalue problem

$$7 \quad V^T U U^T V b_1 = \lambda b_1. \quad (13)$$

9 After the first step, the PLS method iteratively computes other weight vectors.  
 11 When  $a_1$  and  $b_1$  are available, the score vectors can be computed by  $x_1 = Ua_1$ ,  
 11  $y_1 = Vb_1$ , and loadings (first columns of  $M$  and  $N$ ) can be computed by  $m_1 = \frac{U^T x_1}{x_1^T x_1}$   
 13 and  $n_1 = \frac{V^T y_1}{y_1^T y_1}$ , respectively. The data matrices  $U$  and  $V$  are the deflated by sub-  
 13 tracting their rank- one approximation.

$$15 \quad \begin{aligned} U &\leftarrow U - x_1 m_1^T, \\ V &\leftarrow V - y_1 n_1^T. \end{aligned} \quad (14)$$

17 Then new  $U$  and  $V$  are used to compute  $a_2$  and  $b_2$  based on Eqs. (12) and (13).  
 19 This process is repeated until the residuals are small enough or a predefined number  
 21 of weight vectors  $a_1, a_2, \dots, a_p$  and  $b_1, b_2, \dots, b_p$  are obtained.

#### 23 **4. Justification of the Different Stages for RT Process**

25 The basic idea of our work is to track the road in satellite image using PLS–PF. The  
 27 RT algorithm is based on probabilistic modeling of associated data and Bayesian  
 estimation techniques. Basically, RT methods consist of two stages such as predic-  
 29 tion stage and update stage. In our work, PF is used in combination with PLS to  
 recognize and trace various connected road paths and to avoid obstacles under  
 31 various conditions. The PF component is responsible for tracking axis coordinates of  
 a road until it comes to severe obstacles or an intersection. Then, the PLS module  
 33 takes the control of the algorithm and regains track of the road or possibly road  
 branches on the other side of a junction or obstacles. Our work consists of two  
 35 important stages. (i) *K*-means clustering-based seed point selection, and (ii) mea-  
 surement model for object tracking. The overall structure of proposed RT is given in  
 Fig. 1.

##### 37 **4.1. *K*-means clustering-based seed point selection**

39 The basic idea of seed point selection is to give the root to tracking road in satellite  
 41 image which is the initial step to tracking process. In order to apply PF to trace a  
 road in satellite images, we need to consider of the road median on images as a  
 random process. The processing system PF can start its operation from a seed point

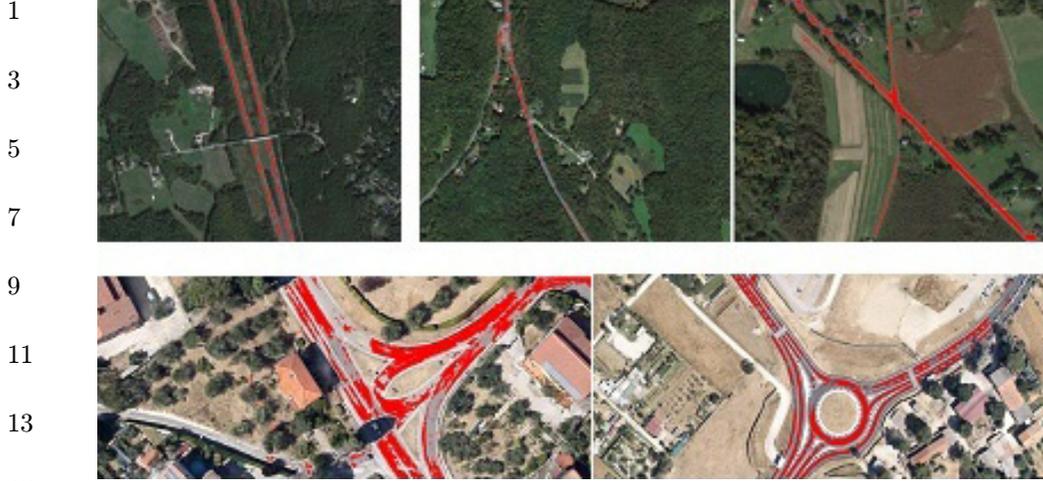


Fig. 1. Five input images.

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(initial point) on the road. This initial point can be provided by a human operator or through automatic approach, this selection is very important to the RT results. In our work, at first, we manually generated reference road model  $R_1$  with is in the form of  $m \times n$  which is helpful for seed point selection. Based on  $R_1$ , we calculate the initial seed point. After that, we split the satellite image into a number of  $m \times n$  the matrix which matrix are converted into a vector format that means each matrix values are arranged into row format. For example,  $n = 7, m = 7$  means we select the reference road model  $R_1$  is in the form of  $7 \times 7$  a matrix. After that we split all the pixel present in the satellite image is converted into  $7 \times 7$  the matrix. Finally, we arrange all matrix into vector format, which vector having the 49 block of vectors. In this vector, we apply the  $K$ -means clustering algorithm for the selection of the initial point of the road which has traced the road path then calculates the minimum distance based on the following objective function.

$$J = \sum_{i=1}^k \sum_{j=1}^n \|x_j^{(i)} - c_i\|^2, \quad (15)$$

where  $\|x_j^{(i)} - c_i\|^2$  is a chosen distance measure between a data point  $x_j^{(i)}$ .  $c_j$  is the cluster center.

For  $K$ -means clustering process, at first, we select the  $k$  initial (in this technique  $k = 10, 15$  and  $20$ ) are randomly generated within satellite image.  $K$ -clusters are generated by associating every observation with the nearest mean. The centroid of each of the  $k$ -clusters becomes the new mean. Which process is repeated until convergence has been reached. Finally, we obtain  $N$  number of centroid and  $N$  number of clusters. After that reference model  $R_1$  is matched with each cluster, one less

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1 Table 3. Pseudo-code for seed point selection.

---

3	<b>Input</b>
	Satellite image
	Parameters of $K$ -means algorithm
5	<b>Output</b>
	Initial seed points in road $R_2$
	<b>start</b>
7	Get the input image $S_{\text{im}}$ from the system
	Randomly select one reference profile $R_1$ which is in the form of $n \times m$ matrix
	Based on the reference point $R_1$ we create the grid structure of input image $S_{\text{im}}$
9	Arrange each grid pixel value into row format based on the grid structure
	<b>Repeat</b>
11	Apply $K$ -means algorithm for initial point selection
	Calculate the minimum distance using Eq. (15)
	For $K$ -means process
13	{
	randomly generated $k$ value from the satellite image
15	$K$ -clusters are generated by associating every observation with the nearest mean.
	The centroid of each of the $K$ -clusters becomes the new mean
	}
17	<b>Repeat</b> the Step 7
	The reference profile $R_1$ is matched with each cluster
	one less distance segment is obtained using Euclidean distance
19	Again, this less distance cluster is matched with grid profile; finally, we obtain one less distance cluster or
	road segment using Euclidean distance.
21	Obtain the seed point $R_2$
	<b>Output</b>
	Initial seed points in road $R_2$
23	<b>end</b>

---

25

27 distance segment is obtained using Euclidean distance. Again, this less distance  
 29 cluster is matched with  $R_1$ , finally, we obtain the one less distance cluster or road  
 31 point  $R_2$  using Euclidean distance. This  $R_2$  is used for the further processing. The  
 33 pseudo-code for seed point selection is given in Table 3.

#### 31 4.2. Measurement model for object tracking

33 The innovative road extraction technique is home to two vital segments such as the  
 35 PF module and the PLS module. The method employed to achieve the measurement  
 37 data differs in each module and is tailored for various roles which each module has to  
 39 play in the overall road extraction technique.

##### 37 4.2.1. Measurement for PF module

39 Subsequent to the seed point choice, we trace the road employing the PF. The  
 41 processing system the PF elegantly commences its functioning from an initial point  
 on the road and subsequently, it sequentially moves to the next point on the road by  
 employing certain synthetically defined time-step. The PF furnishes an effective way

1 to estimate (3) and (4) recursively by means of the Monte Carlo numerical ap-  
 3 proximation techniques. In this innovative technique, the filter evaluates the pos-  
 5 terior density function with the help of a set of arbitrary samples and their matching  
 weights  $(U_K^i, W_K^i)$  named particles. The posterior density is approximated by means  
 of the following relation:

$$7 \quad P(U_K|V_{1:K}) \approx \sum_{j=1}^N W_K^j \delta(U_K - U_K^j). \quad (16)$$

9 When we are able to get sufficient samples from a PDF, the set of samples may be  
 11 deployed to intimately characterize that distribution. Hence, by means of Eq. (16),  
 13 we are able to create the samples  $U_K^i$  directly from the posterior density  $P(U_K|V_{1:K})$ ,  
 15 presuming equal weights  $W_K^i = 1$ . Nevertheless, in actual practice, the captioned  
 17 posterior density does not make its presence every time. Hence, we are able to create  
 19 samples only from certain other density function known as the *importance density  
 function*.<sup>12</sup> Here, by appropriately weighing the sample set, we are able to approxi-  
 21 mate the pdf by utilizing the captioned equation. In an iterative method to the  
 estimation issue, in the course of the  $K$ th step, the set of particles is modernized in  
 accordance with the particles in the prior particles. At the outset, for each  $i = 1 : N$ ,  
 a new particle is sampled from the importance density function as shown below:

21 **Update samples:**

$$23 \quad U_K^i \sim q(U_K|U_{K-1}^i, V_K). \quad (17)$$

25 Subsequently, the importance weights are estimated up to a normalizing constant as  
 27 per the ensuing equation and by employing the matching importance weights from  
 $(K - 1)$ th step

27 **Update weights:**

$$29 \quad \tilde{W}_K^i = W_{K-1}^i \frac{P(V_K|U_K^i)P(U_K^i|U_{K-1}^i)}{q(U_K^i|U_{K-1}^i, V_K)}. \quad (18)$$

31 These weights are adapted by  $W_K^i = \tilde{W}_K^i / \sum_{j=1}^N \tilde{W}_K^j$ . The selection of impor-  
 33 tance density function  $q(U_K|U_{K-1}^i, V_K)$  represents a significant challenge in the de-  
 35 sign of the PF. As far we are concerned, we employ the conventional prior, viz.  
 $P(U_K|U_{K-1}^i)$ , as the importance density function. By means of this selection, (12)  
 and (13) are simplified as detailed below:

37 **Update samples:**

$$39 \quad U_K^i \sim p(U_K|U_{K-1}^i). \quad (19)$$

41 **Update weights:**

$$41 \quad \tilde{W}_K^i = W_{K-1}^i \times p(V_K|U_K^i). \quad (20)$$

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1        At last, the updated particles function as prior for the subsequent state prior  
 3        particles and this recursive function go on till the final state forecast and updating.  
 5        This module generates  $N$  particles from  $R_2$  and continues with the PF algorithm in  
 7        accordance with (17)–(20). Quite different from any occlusion, an intersection or  
 even remarkable change in the road direction the PF concludes the task of tracking.  
 Hence, the PLS is competent to trace the road states in case of harsh occlusion  
 caused in the road.

#### 9        4.2.2. Measurement model for multiple kernels PLS module

11        With an eye on initializing the kernel PLS phase, the PF phase repositions the data  
 13        on its previous victorious step of the current road segment onto the  $k$ -PLS phase. The  
 15        PLS commences its task with a single road branch by employing the previous vic-  
 17        torious state evaluation of the PF phase as its initial point. In the document, we  
 19        regard the RT as a classification issue which marks the target (positive) and back-  
 ground (negative) feature variables with various values. To do the nonlinear task,  
 kernel functions are introduced in PLS algorithm. Here, we combine multiple kernels  
 (MKs) to develop a new hybrid kernel that improves the tracking performance of the  
 system. By introducing the hybrid kernel, PLS can perform flexibility in the form of  
 choice the road points.

21        In hybrid PLS, new hybridized kernel functions are taken and the RT function is  
 23        performed based on this hybrid kernel functions. Let  $k_1$  and  $k_2$  be kernels over  
 $\Xi \times \Xi, \Xi \subseteq R^d$ . Then, three hybrid kernels are formulated based on the definition  
 given in,<sup>20</sup>

- 25        •  $k(x_i, x_j) = k_1(x_i, x_j) + k_2(x_i, x_j)$  is a kernel,
- 27        •  $k(x_i, x_j) = \alpha * k_1(x_i, x_j)$  is a kernel, when  $\alpha > 0$ ,
- $k(x_i, x_j) = k_1(x_i, x_j) * k_2(x_i, x_j)$  is a kernel,

29        In PLS model, we regard the RT as a classification issue which marks the target  
 31        (positive) and background (negative) feature variables with various values. Within  
 33        the PLS formulation, the variables in our RT process comprise two classes such as  
 35        the feature vector and class label. In the ensuing section, we employ  $U \in R^m$  to  
 37        indicate the feature space for object portrayal and  $V \in R$  to signify the class label  
 space for an object. When the target object is identified by means of the PF phase  
 which is deemed as the initial point, we get a positive sample  $u_1$  by extorting a  
 feature vector from the warped image indicated by the state parameter. In case  
 additional positive samples are required for training, we create the virtual data by  
 minimal perturbation and extort the matching feature vectors. With the intent to  
 gather the negative samples, we arbitrarily draw samples from an annular region  
 expressed by  $\gamma < \|O_{\text{neg}} - O\| < \beta$  in which  $O$  represents the target location and  $O_{\text{neg}}$   
 41        characterizes the location of a negative sample. With the achieved road point, we

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1 employ the PLS evaluation to decide an appearance model of the target object. The  
 2 steps involved in object tracking based on  $k$ -PLS are explained follows:

3 **(i) Applying first theorem**

5 Step 1: At first we randomly initialize  $y$

6 Step 2: To calculate the kernel-based score component  $x$

$$7 \quad x = k_{H'} y. \quad (21)$$

9 Step 3: Substitute the first theorems in Eq. (21), here  $k_1$  is radial basis function  
 10 and  $k_2$  is the quadratic kernel. The first theorem to apply Eq. (21), we  
 11 get,

$$12 \quad x = (k_1(x_i, x_j) + k_2(x_i, x_j)) y. \quad (22)$$

13 Step 4: After that to calculate the weight vector  $b_1$  based on Eq. (22)

$$14 \quad b_1 = V^T x \quad (23)$$

$$15 \quad b_1 = V^T ((k_1(x_i, x_j) + k_2(x_i, x_j)) y). \quad (24)$$

17 Step 5: Based on the above equation finally, we calculate  $y = V b_1$

$$18 \quad y = V [V^T ((k_1(x_i, x_j) + k_2(x_i, x_j)) y)], \quad y \leftarrow y / \|y\|. \quad (25)$$

20 Step 6: Repeat Steps 2–6 until convergence

21 Deflate  $(k_1 + k_2)$ ,  $V$  matrices:  $(k_1 * k_2) \leftarrow (k_1 - x x^T k_1)(k_1 - x x^T k_1)^T + (k_2 -$   
 22  $x x^T k_2)(k_2 - x x^T k_2)^T$

$$23 \quad V \leftarrow V - x x^T V. \quad (26)$$

25 **(ii) Applying the second theorem**

26 When applying the second theorem to the PLS, at first, we randomly initialize  $y$   
 27 value. After that, we calculate the kernel-based score component  $x$ .

$$28 \quad x = k_{H''} y \quad (27)$$

29 where

30  $k_{H''} \rightarrow$  Kernel,  $k_{H''} = \alpha * k_1(x_i, x_j)$ .

31 After that, we substitute the kernel value (second theorem) to Eq. (27), we get,

$$32 \quad x = (\alpha * k_1(x_i, x_j)) y. \quad (28)$$

33 After calculating the score component, we calculate the weight vector  $b_1$  based on the  
 34 score component  $x$ .

$$35 \quad b_1 = V^T x, \quad (29)$$

$$36 \quad b_1 = V^T ((\alpha * k_1(x_i, x_j)) y). \quad (30)$$

37 Using above equation, we calculate  $y$  value

$$38 \quad y = V b_1,$$

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$$1 \quad y = V[V^T((\alpha^*k_1(x_i, x_j))y)], \quad y \leftarrow y/\|y\|. \quad (31)$$

3 Deflate  $(\alpha, k_2)$ ,  $V$  matrices:  $(\alpha, k_2) \leftarrow \alpha(k_1 - xx^T k_1)(k_1 - xx^T k_1)^T$

$$V \leftarrow V - xx^T V. \quad (32)$$

### 5 (iii) Applying the third theorem

7 In this section, we explain the third theorem. Here, we use the kernel are  $k_{H''}$  which is  
 7  $k_1(x_i, x_j)^*k_2(x_i, x_j)$ . When we apply the kernel to the PLS, we obtain the output is  
 9 obtained in Eq. (33).

$$9 \quad x = (k_1(x_i, x_j)^*k_2(x_i, x_j))y. \quad (33)$$

11 Using Eq. (33), we calculate the weight vector  $b_1$  based on Eq. (33)

$$13 \quad b_1 = V^T x, \quad (34)$$

$$15 \quad b_1 = V^T((\alpha^*k_1(x_i, x_j))y). \quad (35)$$

17 The above equation is used to calculate the weight vector. Finally, we calculate the  
 17  $y = Vb_1$ ,

$$19 \quad y = V[V^T((\alpha^*k_1(x_i, x_j))y)], \quad y \leftarrow y/\|y\|. \quad (36)$$

21 Deflate  $(k_1 + k_2)$ ,  $V$  matrices:

$$23 \quad (k_1 + k_2) \leftarrow (k_1 - xx^T k_1)(k_1 - xx^T k_1)^T * (k_2 - xx^T k_2)(k_2 - xx^T k_2)^T,$$

$$V \leftarrow V - xx^T V. \quad (37)$$

25 The weight vectors mirror the significance of each original feature variable for  
 27 object portrayal and categorization. If each feature variable in the chosen feature  
 29 space  $U$  represents a function of a pixel location in an object region, then the sig-  
 31 nificance of this feature variable is linked to the discriminability between the target  
 33 and the background classes at a specified location. Hence, we are able to employ  
 35 weight to produce a saliency (importance) map, which illustrates the discriminative  
 caliber of diverse locations in an object region. For instance, if each variable defines  
 the intensity of one pixel and a feature vector signifies the band of pixel intensities in  
 an object region, a subspace can be comprehended by the PLS assessment with  
 certain positive and negative samples.

#### 35 4.2.3. Two-stage RT algorithm

37 The main idea of our proposed approach is to track the road from satellite images  
 39 using PF and multi-kernel particle least square analysis (MK-PLS) algorithms. At  
 41 first, we calculate the initial seed point using  $K$ -means clustering algorithm. Once we  
 calculate the seed point, based on the seed point PF algorithm tracking the road  
 point from the satellite image. The PF component is responsible for tracking axis

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Table 4. Pseudo-code for overall process of RT.

```

1
2
3 Input:
4 The parameter of PF algorithm
5 The parameter of the PLS algorithm
6 The parameter of satellite image
7 output:
8 Road segment
9 Assumption:
10 Input image  $S_{im}$ , initial leader point  $R_{im}$ , weight  $W$ , Probability value  $P_i$ ,  $W_K^i = 1$ .
11 Start
12 Pick up the initial leader point
13 {
14 Randomly select one reference profile  $R_1$  which is in the form of  $n \times m$  matrix
15 Based on the  $R_1$ , create the grid and rearrange the image into a grid format.
16 }
17 Repeat
18 {
19 Apply the  $K$ -means algorithm to the grid image
20 Obtain the seed point  $R_2$ 
21 }
22 for each next point selection apply PF
23 {
24 calculate the posterior density function using (16)
25 Calculate the weight of the point using (18)
26 Predict the next point using (19)
27 Update the next point using (20)
28 }
29 Repeat
30 If there is an obstacle in the road; stop the criteria
31 Then
32 {
33 Continues the tracking process using hybrid kernel-based PLS algorithm
34 }
35 for each next point selection
36 {
37 Get the input from the PF
38 Select the target (positive) and background (negative) value
39 Calculate the weight matrix
40 Apply the multiple to each point
41 Obtain the next point}
42 Repeat still road is segmented from the  $S_{im}$ .
43 Stop
44 Output:
45 Segmented road
46 end

```

37

39 coordinates of a road until it comes to severe obstacles or an intersection. If any  
41 obstacles arrive means the process is continued using the MK-PLS algorithms. The  
42 MKs are combined with PLS algorithm still road is tracked from the image which  
43 improves the tracking performance.

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## 1 5. Result and Discussion

3 We now describe the result of experimentation using our proposed framework. The  
 5 performance of the proposed method is verified using satellite images of size  $512 \times$   
 7  $512$  each. The dataset (250 images) used here consists of five categories of satellite  
 9 images, with 50 per category. This is split equally into two parts — one (125) used for  
 11 training and another for testing. The performance of proposed techniques is com-  
 pared with different state-of-the-art techniques. The proposed technique is per-  
 formed in a windows machine having configurations Intel (R) Core i5 processor,  
 3.20 GHz, 4 GB RAM, and the operating system platform is Microsoft Window 7  
 Professional. We have used MATLAB latest version (7.12) for this proposed  
 technique.

### 13 5.1. Data set description and performance measures

15 We have elegantly generated a database for the satellite image with  $1-m/\text{pixel}$   
 17 resolution from *Wikimedia*. The quality of the image is dependent on the sensor  
 19 employed in the climatic situations. For this experimentation, we used the five  
 21 types of satellite images. The input image size is  $1200 \times 900$  pixels. To assess the  
 performance of the road extraction system in this work, we utilize the four eval-  
 uation measures such as accuracy, sensitivity, specificity, completeness and  
 correctness.

23 **Sensitivity:** Sensitivity is the proportion of true positives that are correctly iden-  
 25 tified by a proposed method. It shows how good the test is at detecting a road.

$$27 \text{Sensitivity} = \frac{\text{TP}}{\text{TP} + \text{FN}} . \quad (38)$$

31 **Specificity:** Specificity is the proportion of the true negatives correctly identified by  
 33 proposed method. It suggests how good the test is at identifying the normal (nega-  
 35 tive) condition.

$$37 \text{Specificity} = \frac{\text{TN}}{\text{TN} + \text{FP}} . \quad (39)$$

39 **Accuracy:** Accuracy is the proportion of true results, either true positive or true  
 41 negative, in a population.

$$43 \text{Accuracy} = \frac{\text{TN} + \text{TP}}{\text{TN} + \text{FP} + \text{FN} + \text{FP}} . \quad (40)$$

45 **Completeness:** Completeness is defined as the percentage of the reference data  
 47 which was detected during road extraction.

$$49 \text{Completeness} = \frac{\text{length of matched reference}}{\text{length of reference}} . \quad (41)$$

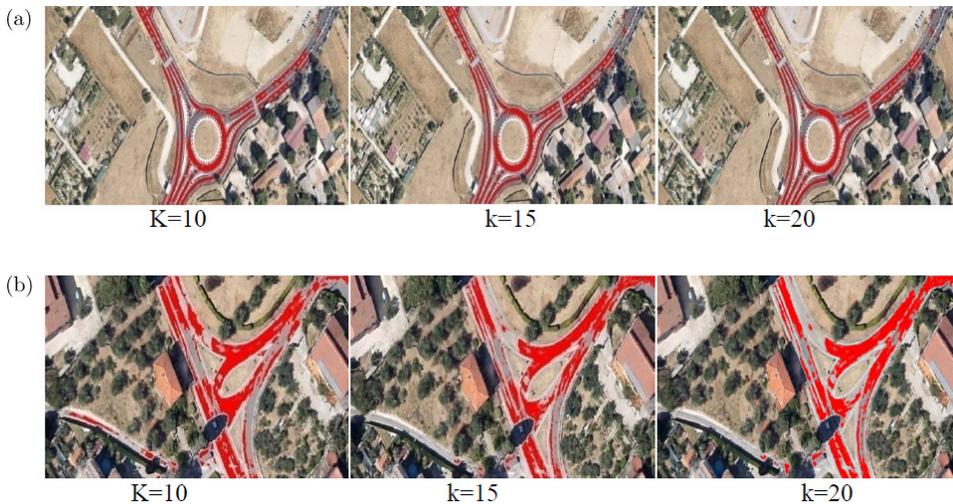
1 **Correctness:** Correctness represents the percentage of the extracted road data  
 2 which is correct

$$3 \text{ Correctness} = \frac{\text{length of matched extraction}}{\text{length of extraction}}. \quad (42)$$

## 7 5.2. Experimental results

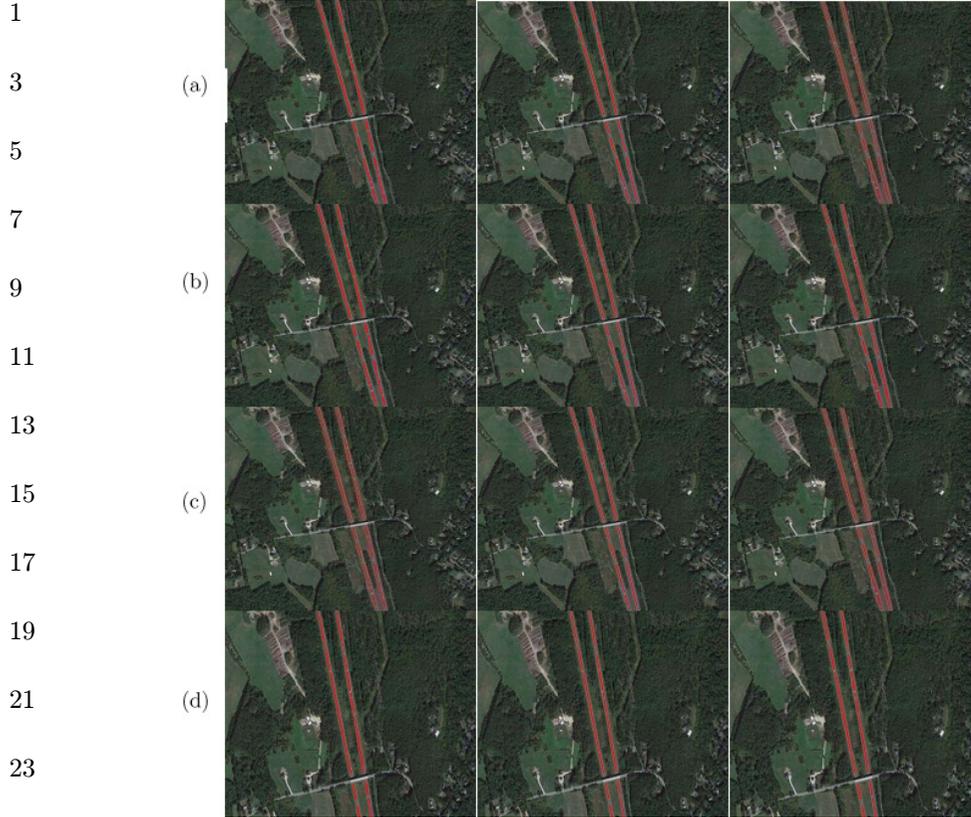
8 The basic idea of our research is to track the road based on the MK-PLS analysis  
 9 with PF from the satellite images. To evaluate the performance of our proposed  
 10 approach, we compare our results with different approaches. We have chosen five  
 11 images to show in detail behavior of the proposed approach. In the five images, a  
 12 sinuous but very homogeneous road is shown. The RT performance of proposed and  
 13 previous approach with three images is presented. In our work, at first, we calculate  
 14 the initial point of the road using  $K$ -means clustering algorithm. This initial point is  
 15 used to further track the road accurately. Based on the clusters, the tracking process  
 16 is started. Figure 2 shows the performance of the satellite image using different  
 17 cluster values.

18 In our work, we use a different kernel with PLS. At first, we apply the PF to the  
 19 initial point to obtain the tracking the road. If any obstacles are present in the road  
 20 the PF stops the process. After that, the ending point itself the PLS start the process.  
 21 The PLS address the poor generalization properties, so overcome this problem we  
 22 utilize kernel with PLS algorithm. Further, improve the performance of the RT in  
 23 our work we utilize the two types of kernels (quadratic kernel and radial basis



42 Fig. 2. Results obtained from proposed approach using PF+ MK-PLS for different cluster values  
 43 (a) image 1 and (b) image 2.

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**Fig. 3.** (a) Results obtained from proposed approach using Theorem 1, (b) result obtained from using Theorem 2 and (c) result obtained from using Theorem 3 in image 1.

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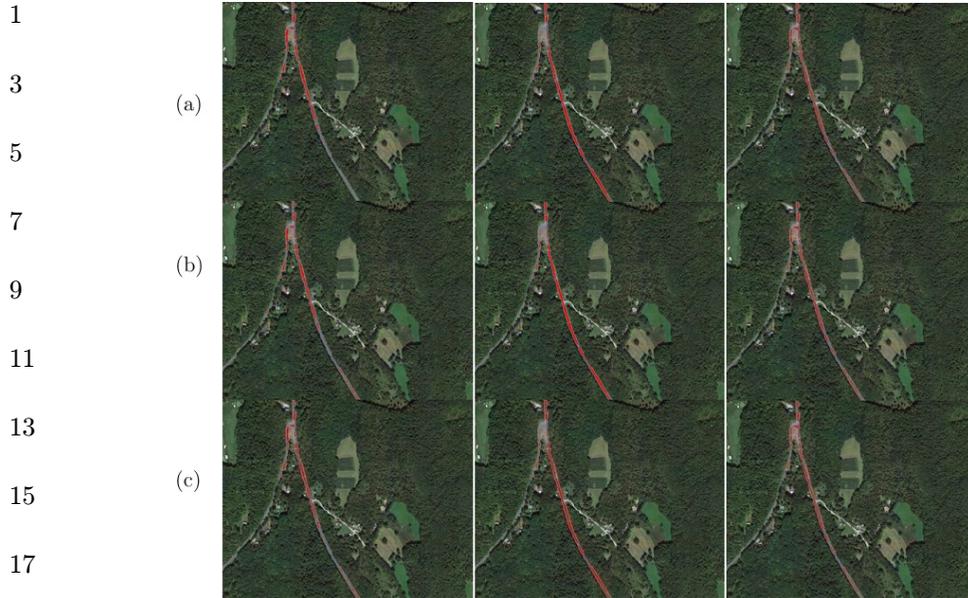
function) with PLS. Finally, we obtain the road map from the satellite image without information losing. Figures 3–5 show the experimental result of RT using different approaches. In this experiment, we utilize the three types of the image; each image having three cluster values these are shown in the corresponding image.

### 5.3. Performance evaluation

In this section, we provide the performance of the proposed approach using three types of theorems. Here, we employ five benchmark functions in our work which are explained in Eqs. 38–42. We choose these benchmark functions because they are being widely used by many researchers in the study of RT. The experimentation carried out five different types of satellite images to take our RT process. The result obtained by using three types of the theorem shown in Tables 5–9.

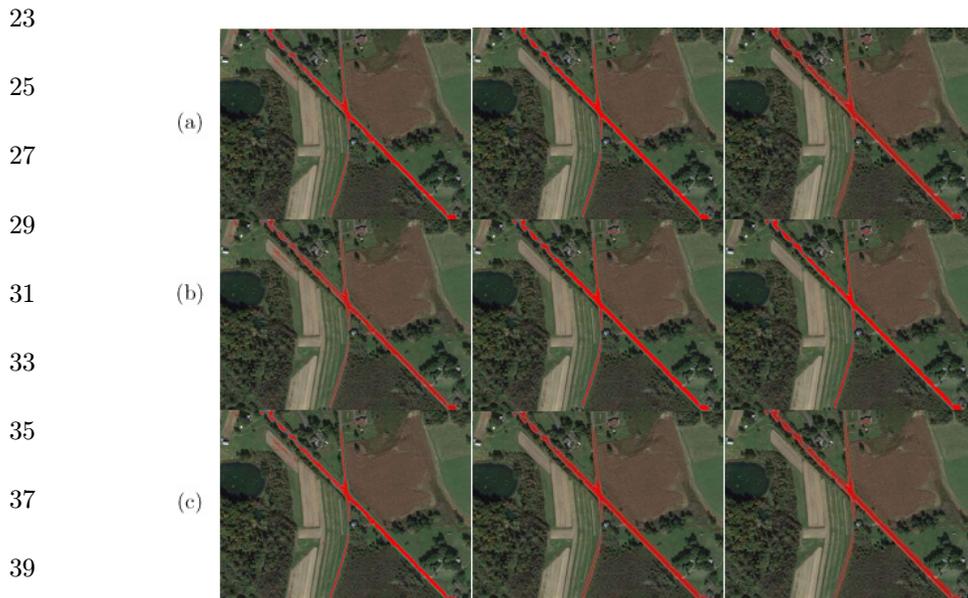
To evaluate the performance of our proposed approach, we compare our result with different theorems. Here, each theorem using the different kernels such as radial

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19 **Fig. 4.** (a) Results obtained from proposed approach using Theorem 1, (b) result obtained from using  
21 Theorem 2 and (c) result obtained from using Theorem 3 in image 2.

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41 **Fig. 5.** (a) Results obtained from proposed approach using Theorem 1, (b) result obtained from using  
Theorem 2 and (c) result obtained from using Theorem 3 in image 3.

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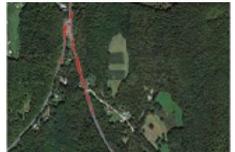
1 Table 5. Performance comparison table for using different theorems in image 1.

3 Images	No. of clusters	Performance measures	Theorem 1	Theorem 2	Theorem 3
5 	10	Accuracy	98.0917	98.2237	98.1857
		Completeness	98.5769	98.7308	98.714
		Correctness	95.5989	95.7309	95.6929
		Sensitivity	22.8665	28.1938	26.6571
		Specificity	99.9997	100	100
9 	15	Accuracy	98.309	98.0832	98.106
		Completeness	98.8041	98.5786	98.5952
		Correctness	95.8162	95.5904	95.6132
		Sensitivity	31.6412	22.5131	23.4351
		Specificity	100	100	100
13 	20	Accuracy	98.2224	98.2151	98.2077
		Completeness	98.7099	98.7112	98.709
		Correctness	95.7304	95.7223	95.715
		Sensitivity	28.158	27.8455	27.5484
		Specificity	99.9996	100	100

19

21

23 Table 6. Performance comparison table for using different theorems in image 2.

25 Images	No. of clusters	Performance measures	Theorem 1	Theorem 2	Theorem 3
27 	10	Accuracy	98.2963	98.1778	98.1634
		Completeness	98.5526	98.4008	98.3936
		Correctness	96.3294	96.212	96.1975
		Sensitivity	16.813	11.0591	10.3543
		Specificity	100	99.9993	99.9993
31 	15	Accuracy	98.2698	98.3304	98.3152
		Completeness	98.5358	98.6218	98.6138
		Correctness	96.3029	96.3635	96.3483
		Sensitivity	15.5187	18.4789	17.7356
		Specificity	100	100	100
35 	20	Accuracy	98.1386	98.1799	98.1861
		Completeness	98.3735	98.44	98.4443
		Correctness	96.1717	96.213	96.2192
		Sensitivity	9.1113	11.1296	11.4308
		Specificity	100	100	100

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1 Table 7. Performance comparison table for using different theorems in image 3.

3 Images	No. of clusters	Performance measures	Theorem 1	Theorem 2	Theorem 3
5 	10	Accuracy	97.5798	97.5815	97.4885
		Completeness	98.435	98.2766	98.2279
		Correctness	95.0932	95.0875	94.9905
		Sensitivity	40.228	37.4734	35.0028
		Specificity	99.8314	99.9413	99.9416
9 	15	Accuracy	97.9424	98.0003	98.037
		Completeness	98.6519	98.6849	98.6981
		Correctness	95.4428	95.5023	95.5393
		Sensitivity	46.2605	47.8901	48.9217
		Specificity	99.9714	99.9676	99.9652
15 	20	Accuracy	98.0305	97.991	97.9262
		Completeness	98.7396	98.7152	98.6933
		Correctness	95.5359	95.5004	95.4308
		Sensitivity	48.7498	47.8041	45.969
		Specificity	99.9652	99.9613	99.966

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25 Table 8. Performance comparison table for using different theorems in image 4.

27 Images	No. of clusters	Performance measures	Theorem 1	Theorem 2	Theorem 3
27 	10	Accuracy	97.9424	98.0003	98.037
		Completeness	98.6519	98.6849	98.6981
		Correctness	95.4428	95.5023	95.5393
		Sensitivity	46.2605	47.8901	48.9217
		Specificity	97.9424	98.0003	98.037
31 	15	Accuracy	98.0917	98.2237	98.1857
		Completeness	98.5769	98.7308	98.714
		Correctness	95.5989	95.7309	95.6929
		Sensitivity	22.8665	28.1938	26.6571
		Specificity	100	100	100
35 	20	Accuracy	97.5798	97.5815	97.4885
		Completeness	98.435	98.2766	98.2279
		Correctness	95.0932	95.0875	94.9905
		Sensitivity	40.228	37.4734	35.0028
		Specificity	97.5798	97.5815	97.4885

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Table 9. Performance comparison table for using different theorems in image 5.

Images	No. of clusters	Performance measures	Theorem 1	Theorem 2	Theorem 3
	10	Accuracy	98.1386	98.1799	98.1861
		Completeness	98.3735	98.44	98.4443
		Correctness	96.1717	96.213	96.2192
		Sensitivity	9.1113	11.1296	11.4308
		Specificity	100	100	100
	15	Accuracy	98.2151	98.2077	98.2224
		Completeness	98.7112	98.709	98.7099
		Correctness	95.7223	95.715	95.7304
		Sensitivity	27.8455	27.5484	28.158
		Specificity	100	100	99.9996
	20	Accuracy	97.9424	98.0003	98.037
		Completeness	98.6519	98.6849	98.6981
		Correctness	95.4428	95.5023	95.5393
		Sensitivity	46.2605	47.8901	48.9217
		Specificity	97.9424	98.0003	98.037

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basis function and quadratic kernel. From Tables 5–9, we obtain the average accuracy of 98.004% for Theorem 1, 98.024% for Theorem 2 and 98.087% for Theorem 3 for cluster size 10. In this approach, the kernel function is used to improve the performance of the proposed approach.

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#### 5.4. Comparative analysis

To evaluate the performance of our proposed approach, we compare our results with our previous methods. Here, we compare our work with four approaches such as EKF+PF,<sup>40</sup> LEGION,<sup>50</sup> UKF+GHKF<sup>45</sup> and LEGION+GHKF.<sup>46</sup> Furthermore, these approaches characterize the local features of the road, based on the initial point, visual features and contrast. Therefore, we have chosen to compare the performance of our proposed algorithm against that of these ones. In Ref. 40, the author explained the road extraction from satellite image based on PF and EKF (PF+EKF). This method very well explains the RT, even though the deficiency of the algorithm is slow for PF module and it is more complex for urban areas. In Ref. 50, the author explained the LEGION-based automatic road extraction from a satellite image. This LEGION method is not very sensitive to particular parameters. In our first paper,<sup>45</sup> we extract the road from satellite image using UKF and GHKF. This method is efficient for road extraction even though it takes a lot of time. By reducing the process time and improving the extracted details, in our second paper, we introduced LEGION and GHKF-based road extraction from high-resolution satellite images.<sup>46</sup> To overcome the complexity present in the above methods, we further introduced the proposed method. From the result, one can observe that LEGION+GHKF<sup>46</sup> method and our

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1 proposed one yield the best performance followed by EKF+PF,<sup>40</sup> UKF+GHKF<sup>45</sup> and  
 2 LEGION.<sup>50</sup> This is because these methods very well describe the features of the  
 3 satellite image. Compared to LEGION+GHKF<sup>46</sup> method our proposed method is  
 4 slightly better<sup>46</sup> because of the use of hybrid kernel. To prove the effectiveness of the  
 5 approach, we compare our proposed work with different measures such as accuracy,  
 6 completeness and correctness.

7 Tables 10–14 shows the comparative analysis of proposed approach based on  
 8 different measures. Table 10 shows the performance of proposed approach against  
 9 existing approaches such as EKF+PF,<sup>40</sup> UKF+GHKF,<sup>45</sup> LEGION<sup>50</sup> and  
 10 LEGION+GHKF<sup>46</sup> for image 1. In Table 6, when the cluster value is 20, we obtain  
 11 the maximum accuracy of 98.4 for proposed approach which is 97.0 using  
 12 EKF+PF,<sup>40</sup> 97.2 using UKF+GHKF,<sup>45</sup> 97.4 using LEGION<sup>50</sup> and 97.9 using  
 13 LEGION+GHKF.<sup>46</sup> The performances in terms of completeness and correctness  
 14 measures at the different clustering stages of proposed against existing approach also  
 15 given in Table 10. When analyzing this measures, our proposed approach achieves  
 16 the high completeness of 98.4 and high correctness of 95.8. Moreover, Table 11 shows  
 17 the comparative analysis of proposed approach against existing work for image 2.  
 18 From Table 11, we can view all the methods are more or equal accuracy value. In the  
 19 method LEGION+GHKF<sup>46</sup> having the maximum accuracy of 98.5 which is slightly  
 20 better than our proposed method. The higher completeness value is producing the  
 21 better performance of the tracking process. The performance in terms of correctness  
 22 measure at different clustering stages of proposed against existing approach also  
 23 shown in Table 11.

25 Table 10. Comparative analysis of proposed approach based on different measures for image 1.

Measures	Accuracy			Completeness			Correctness		
	10	15	20	10	15	20	10	15	20
Cluster size									
EKF+PF <sup>40</sup>	97.5	97.6	97.0	97.7	98.0	97.5	95.0	95.1	95.3
LEGION <sup>50</sup>	98.1	98.1	97.4	98.7	98.8	98.7	95.7	95.7	95.7
UKF+GHKF <sup>45</sup>	98.2	98.2	97.2	1.0	1.0	0.76	95.6	95.6	95.3
GHKF+LEGION <sup>46</sup>	98.2	98.2	97.9	98.7	98.0	98.7	95.7	95.7	95.7
PF+MK-PLS	98.3	98.2	98.4	102.4	102.3	102.4	96.6	96.6	96.7

33 Table 11. Comparative analysis of proposed approach based on different measure for image 2.

Measures	Accuracy			Completeness			Correctness		
	10	15	20	10	15	20	10	15	20
Cluster size									
EKF+PF <sup>40</sup>	97.9	97.9	97.9	97.9	98.3	97.9	95.9	95.9	95.9
LEGION <sup>50</sup>	98.2	98.4	98.4	98.8	98.7	98.7	96.4	96.4	96.4
UKF+GHKF <sup>45</sup>	97.9	98.2	98.2	0.1	0.5	0.4	95.9	96.2	96.2
GHKF+LEGION <sup>46</sup>	98.5	98.4	98.4	98.9	98.8	98.7	96.5	96.4	96.4
PF+MK-PLS	98.3	98.5	98.3	102.2	102.4	102.3	97.2	97.3	97.2

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1 Table 12. Comparative analysis of proposed approach based on different measures for  
2 image 3.

3	Measures	Accuracy			Completeness			Correctness		
5	Cluster size	10	15	20	10	15	20	10	15	20
6	EKF+PF <sup>40</sup>	96.5	96.2	96.6	97.5	96.4	97.8	93.9	93.7	94.0
7	LEGION <sup>50</sup>	97.3	97.5	97.5	98.1	98.4	98.4	95.6	94.5	95.6
8	UKF+GHKF <sup>45</sup>	98.1	97.0	98.1	2.8	2.1	2.8	94.8	95.1	95.1
9	GHKF+LEGION <sup>46</sup>	97.5	97.6	97.6	98.4	98.6	98.6	94.9	95.2	95.1
10	PF+MK-PLS	9.7	98.6	98.2	101.9	102.2	102.3	96.0	96.3	96.5

11 Similarly, performance in terms of accuracy, completeness and correctness mea-  
12 sure at different clustering stages of our proposed framework for image 3 is shown in  
13 Table 12. In Table 12, our proposed work achieves the maximum accuracy of 98.6  
14 which is 97.6 for using LEGION+GHKF,<sup>46</sup> 97.5 for using LEGION,<sup>50</sup> 97 for using  
15 UKF+GHKF<sup>45</sup> and 96.2 for using EKF+PF.<sup>40</sup> Similarly, we obtain the maximum  
16 completeness of 98.4 and correctness of 95.6. From Table 12, we clearly understand  
17 our proposed approach achieves the maximum accuracy, completeness, and cor-  
18 rectness compared to the existing approaches. Moreover, Table 13 shows the per-  
19 formance of proposed approach against existing approaches such as EKF+PF,<sup>40</sup>  
20 UKF+GHKF,<sup>45</sup> LEGION<sup>50</sup> and LEGION+GHKF<sup>46</sup> for image 4. Here, when used  
21 cluster value is 15, we obtain the maximum accuracy of 91.4 which is high compared  
22 to EKF+PF,<sup>40</sup> UKF+GHKF,<sup>45</sup> LEGION<sup>50</sup> and LEGION+GHKF.<sup>46</sup> The methods

23 Table 13. Comparative analysis of proposed approach based on different measures for  
24 image 4.

25	Measures	Accuracy			Completeness			Correctness		
27	Cluster size	10	15	20	10	15	20	10	15	20
28	EKF+PF <sup>40</sup>	90.5	90.6	90.7	92.1	92.1	92.2	88.2	88.2	88.3
29	LEGION <sup>50</sup>	90.7	90.8	90.8	92.2	92.2	92.3	88.3	88.5	88.4
30	UKF+GHKF <sup>45</sup>	90.6	90.6	90.8	92.3	92.2	92.1	88.2	88.3	88.4
31	GHKF+LEGION <sup>46</sup>	90.9	90.9	91.1	92.1	92.2	92.3	88.6	88.5	88.8
32	PF+MK-PLS	91.3	91.4	91.5	91.8	91.8	91.9	88.8	88.8	88.9

33 Table 14. Comparative analysis of proposed approach based on different measures for  
34 image 5.

35	Measures	Accuracy			Completeness			Correctness		
37	Cluster size	10	15	20	10	15	20	10	15	20
38	EKF+PF <sup>40</sup>	85.9	85.2	85.4	88.7	88.1	88.4	81.8	80.9	81.3
39	LEGION <sup>50</sup>	86.5	85.6	85.7	88.7	88.1	88.5	81.5	81.1	81.3
40	UKF+GHKF <sup>45</sup>	85.6	85.2	85.4	88.8	88.2	88.5	82.4	81.5	81.6
41	GHKF+LEGION <sup>46</sup>	86.3	86.1	86.2	88.7	88.3	88.5	82.2	81.9	82.1
42	PF+MK-PLS	87.3	86.5	86.8	88.2	87.6	87.9	83.9	82.1	82.5

1 EKF+PF<sup>40</sup> are UKF+GHKF<sup>45</sup> obtain the most similar result using all the stages.  
2 The performance in terms of accuracy, completeness and correctness measures at  
3 different clustering stages of our proposed framework using image 5 is shown in  
4 Table 14. When using the cluster value is 20, we obtain the maximum accuracy of  
5 86.8 which is very much high compared to the existing approach. From the entire  
6 above table, we clearly understand our proposed approach obtains the better results  
7 compared to other approaches.

## 9 6. Conclusion

10 We have developed an efficient algorithm based on a kernel hybridization for PLS  
11 analysis with PF as a RT approach for satellite images. At first, we calculate the  
12 initial leader point using  $K$ -means clustering algorithm which is useful for the further  
13 processing. After that, the PF traces a road still a stopping benchmark is satisfied.  
14 Subsequently, the hybrid kernel-based PLS algorithm performs the remaining LRT.  
15 To reduce the tracking drift, we using hybrid kernels such as the linear kernel and  
16 polynomial kernel with PLS approach. Compared with state-of-the-art tracking  
17 methods, the proposed algorithm achieves favorable performance with higher accu-  
18 racy and lower tracking errors.

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